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Electroluminescence efficiencies of erbium in silicon-based hosts

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We report on room-temperature 1.5 μm electroluminescence from trivalent erbium (Er^{3+}) ions embedded in three different CMOS-compatible silicon-based hosts: SiO_2 , Si_3N_4 , and SiN_x . We show that although the insertion of either nitrogen or excess silicon helps enhance electrical conduction and reduce the onset voltage for electroluminescence, it drastically decreases the external quantum efficiency of Er^{3+} ions from 2% in SiO_2 to 0.001% and 0.0004% in SiN_x and Si_3N_4 , respectively. Furthermore, we present strong evidence that hot carrier injection is significantly more efficient than defect-assisted conduction for the electrical excitation of Er^{3+} ions. These results suggest strategies to optimize the engineering of on-chip electrically excited silicon-based nanophotonic light sources.
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Research towards fabricating efficient electrically driven silicon-based light sources holds promise for the full integration of nanophotonics with microelectronics on a silicon chip.¹ To circumvent the intrinsically low photon emission probability in silicon, researchers have investigated methods to dope silicon-based host materials with more efficient light emitters.^{2–4} For this purpose, Er^{3+} ions have attracted considerable interest because their near-infrared 1.5 μm emission coincides with the “C-band” of optical telecommunication.⁵ In silicon though, Er^{3+} ions undergo significant thermal quenching due to non-radiative energy back-transfer to the host matrix.³ Strategies to avoid such electronic back-transfer consist of using large bandgap silicon-based hosts such as SiO_2 or Si_3N_4 . While these latter host materials were shown to be a good platform for Er^{3+} photoluminescence, their insulating properties impede carrier injection and transport for electrically-driven devices.

To address this electrical challenge, researchers have sought to embed Er^{3+} ions in engineered host materials that allow for efficient injection of carriers at low operating voltages. For example, recent studies investigated the influence of host composition on the electroluminescence (EL) properties of $\text{Er}^{3+}:\text{SiN}_x$ (Ref. 6) and $\text{Er}^{3+}:\text{SiO}_x$ (Refs. 7–9) as well as other oxide hosts such as $\text{Er}^{3+}:\text{TiO}_2$ (Ref. 10) and $\text{Er}^{3+}:\text{ZnO}$.^{11,12} However, it can be difficult to interpret and resolve the conflicting results reported in the literature because of the disparities in electrical and optical properties between different hosts as well as the fabrication-dependent properties observed for similar materials.^{13,14}

In this letter, we report on a systematic comparison of several figures of merit for Er^{3+} EL in different silicon-based CMOS-compatible hosts. To this end, we investigate the

electrical and optical properties of Er-doped electroluminescent devices fabricated with three distinct hosts for the active layer: silicon dioxide (SiO_2), silicon nitride (Si_3N_4), and silicon-rich nitride (SiN_x). By using the same fabrication equipment, processing techniques, and device geometry (e.g., emitter layer thickness and area) for all samples, we seek to isolate the host material dependencies of the Er-doped active layers. While all devices display 1.5 μm emission under electrical injection, we show that their respective properties such as external quantum efficiency, electrical transport characteristics, and excitation cross-sections significantly differ, sometimes by orders of magnitude.

The Er-doped Si-based active layers were all deposited by the same confocal magnetron sputtering equipment at high substrate temperature (500 °C).¹⁵ Near stoichiometric $\text{Er}^{3+}:\text{SiO}_2$ and $\text{Er}^{3+}:\text{Si}_3\text{N}_4$ were produced by cosputtering from Er_2O_3 and either SiO_2 or Si_3N_4 targets under a plasma of pure argon. $\text{Er}^{3+}:\text{SiN}_x$ was grown using reactive sputtering by flowing 0.6 sccm of nitrogen and 10 sccm of argon inside the chamber during cosputtering of Si and Er_2O_3 targets. The resulting SiN_x host is silicon-rich with $x \approx 0.8$.¹⁶ All active layers are 50 nm-thick and deposited on a p-type silicon substrate ($1 \times 10^{15} \text{ at./cm}^3$). The Er concentration, as measured by secondary ion mass spectrometry (SIMS), was typically found to be around $[\text{Er}] = 1 \times 10^{20} \text{ cm}^{-3}$. A heavily doped ($1 \times 10^{20} \text{ cm}^{-3}$) 100-nm thick n^+ -polysilicon top electrode is subsequently deposited directly on top of the active layer by low pressure chemical vapor deposition (LPCVD). The devices are then post-annealed at 950 °C for 30 min under pure N_2 . To form electrical contacts, aluminum and chromium were deposited on the top and bottom of the structure, respectively; the top aluminum contacts were patterned in the shape of isolated squares (200 μm by 200 μm) with empty square center (60 μm by 60 μm) to allow for efficient electrical excitation and light extraction (a sketch of the device is shown inset of Fig. 1(a)). All electro-optical

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experiments were performed under forward bias (i.e., negative voltage applied to the polysilicon electrode) allowing higher current to flow through the active layer. A probe station and a semiconductor device analyzer were used to monitor I–V characteristics. The electroluminescence signal was collected from the top half of the device through the Si electrode by a microscope objective (NA: 0.4). For spectral analysis, the light was dispersed by a spectrograph and measured with a calibrated photomultiplier tube (PMT). Time-resolved measurements were carried out using a pulse generator, and EL decay traces were recorded with a digital GHz oscilloscope connected to the PMT.

Figure 1 displays both the current density and the EL signals of the three layers investigated as a function of the applied voltage (until reaching the electrical breakdown of the active layer). A typical EL spectrum is displayed in the inset of Fig. 1(b); the EL spectrum for all samples showed a similar line shape. One can readily observe a clear trend in the electrical properties when nitrogen is introduced and when Si-excess content is increased: as shown in Fig. 1(a), the threshold voltage is decreased, and the maximum current density is enhanced. Consequently, as shown in Fig. 1(b), the onset voltage for EL is strongly reduced, from ~ 45 V to

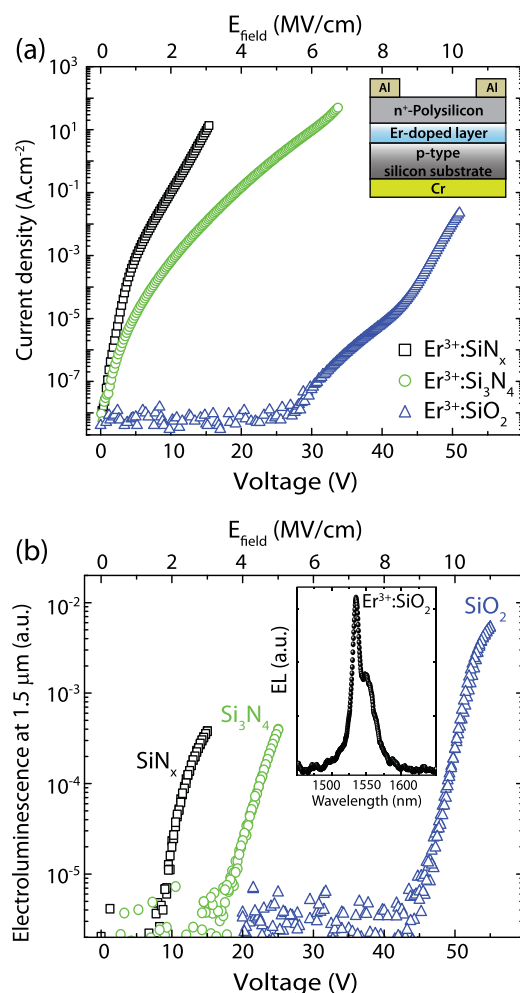


FIG. 1. (a) Current density as a function of the applied voltage for $\text{Er}^{3+}:\text{SiN}_x$, $\text{Er}^{3+}:\text{Si}_3\text{N}_4$, and $\text{Er}^{3+}:\text{SiO}_2$. Inset: scheme of the device's geometry. (b) Electroluminescence intensity at $1.5\ \mu\text{m}$ for the same devices as a function of the applied voltage. Inset: typical EL spectrum obtained (only $\text{Er}^{3+}:\text{SiO}_2$ is displayed for clarity).

~ 7 V, when the composition of the host changes from SiO_2 to SiN_x . However, a collateral effect is that the maximum EL intensity is reduced by around one order of magnitude. At this stage, it is unclear whether it is due to the observed disparities in breakdown voltages or to intrinsic differences in the active layers' properties, and we therefore provide in the following a thorough investigation of the underlying physical mechanisms involved in this process.

A typical figure of merit for electroluminescence efficacy is external quantum efficiency (EQE), which is given by the ratio between emitted photons and injected electrons. Using a calibrated PMT, the EQE values were obtained as a function of current density. As shown in Figure 2, the EQE of $\text{Er}^{3+}:\text{SiO}_2$ (2%) is three orders of magnitude higher than those of $\text{Er}^{3+}:\text{SiN}_x$ ($10^{-3}\%$) and $\text{Er}^{3+}:\text{Si}_3\text{N}_4$ ($4 \times 10^{-4}\%$). Although all fabricated electroluminescent devices have identical device geometries, the material into which Er^{3+} ions are embedded alters the coupling to radiative modes through two effects: (i) changes in the local field around Er^{3+} and (ii) modification of the Fresnel coefficients at the interfaces.^{17–20} These combined effects imply that increasing the host refractive index should enhance the power radiated to the upper half space of the structure and thus collected by our detection system (see supplementary material²¹). This trend is not observed in our measurements, in which the lowest refractive index ($n_{\text{SiO}_2} = 1.5$) yields the highest EQE. Such a statement indicates that the differences in the measured EQE do not arise from optical effects caused by the change of refractive index but rather from different excitation efficiencies. Further insight is given hereafter through analysis of both electrical transport and excitation cross sections of the Er^{3+} ions.

Due to the dielectric and amorphous character of the active medium, the electrical transport of carriers in such insulating layers typically shows a non-Ohmic behavior. To describe the conduction properties, a whole range of models are available in the literature among which the most commonly reported are Fowler-Nordheim Tunneling²² (FNT) and Poole-Frenkel (PF) thermionic emission.²³ As displayed in Figure 3, we find that the electrical transport in nitride-based layers is a bulk-limited process assisted by localized

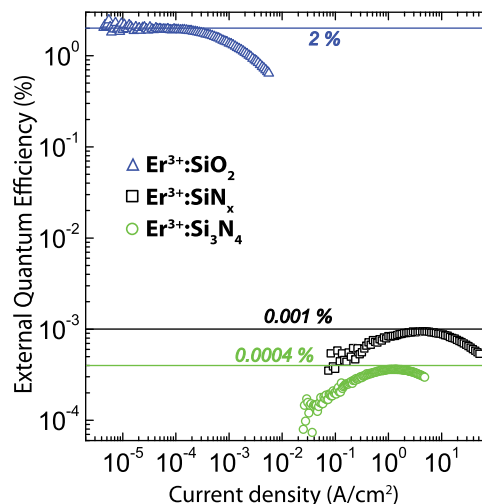


FIG. 2. EQE for the near-infrared emission ($1.3\ \mu\text{m}$ – $1.6\ \mu\text{m}$) as a function of injected current for the three investigated light emitting devices.

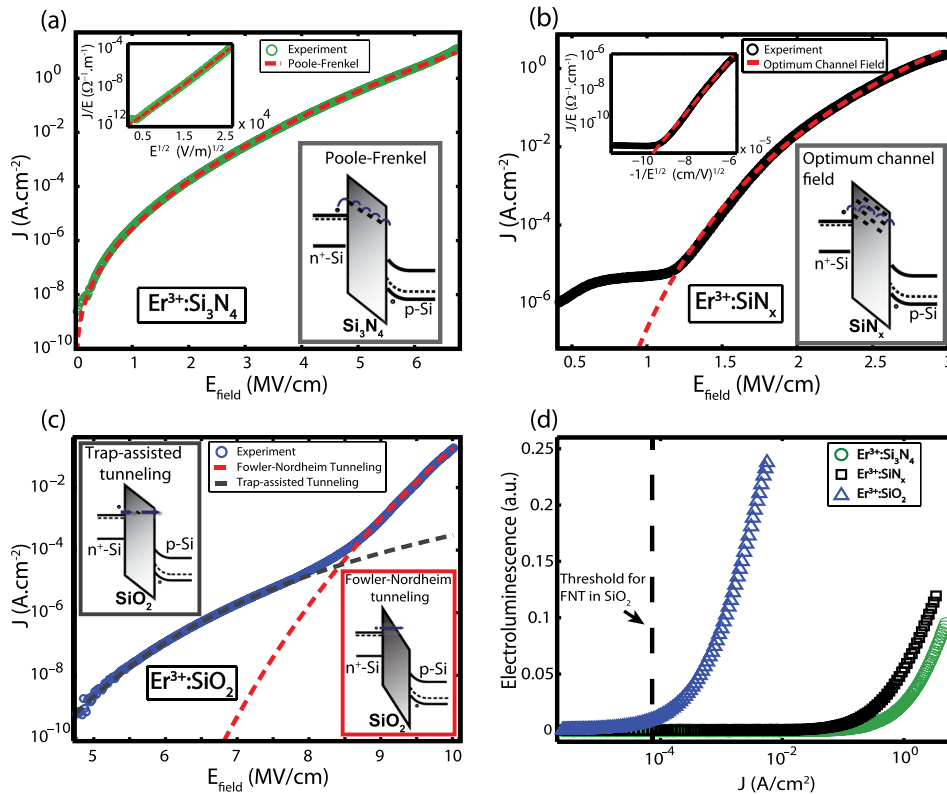


FIG. 3. Current density-electric field (J - E) characteristics response of (a) Er³⁺:Si₃N₄, (b) Er³⁺:SiN_x, and (c) Er³⁺:SiO₂ together with fits from theoretical models. Insets: schematics highlighting the modeled conduction mechanisms. (d) Electroluminescence signal at 1.5 μm as a function of current density.

states in the bandgap, consistent with a previous study.²⁴ Specifically, the J - E curves are best described by PF conduction²⁵ and optimum-channel field emission^{26,27} for Er³⁺:Si₃N₄ and Er³⁺:SiN_x, respectively (more information in the supplementary material²¹). On the other hand, the electrical transport in SiO₂ is first enabled by trap-assisted tunneling (from 5 to 8 MV/cm) and subsequently followed by hot carrier injection due to FNT mechanism at high fields (greater than 8 MV/cm). Interestingly in this latter case, the resulting EL signal starts to be significant only after reaching the FNT regime (see Fig. 3(d)). This suggests that the injection of hot electrons in the conduction band is a more efficient process for the excitation of Er³⁺ ions than trap-assisted conduction.

The excitation cross section of Er³⁺ ions is a key parameter to understand the efficiency of the excitation process under electrical pumping. Er³⁺ ions comprise numerous excited states that usually require a detailed set of rate equations to provide accurate modeling of the electronic transitions.²⁸ However, in the low pump regime, two reasonable assumptions can be made: (i) non-radiative relaxation from higher lying states is much faster than the long relaxation from ⁴I_{13/2} level and (ii) there are no non-linear processes (e.g., excited state absorption or energy transfer between ions). At low current flux, we can therefore model the system under study as a quasi-two-level-system even if the excitation occurs at higher-lying states (see supplementary material²¹).²⁹ Therefore, in the steady-state regime, the electroluminescence intensity is described by $EL = \frac{\sigma_{\text{ex}}^L \tau}{\sigma_{\text{ex}}^L \tau + 1} EL_{\text{max}}$.³⁰ By measuring separately the lifetime τ of our samples, the excitation cross-section σ can be extracted by fitting the measured EL signal as a function of the current flux (J/q). It is found that the σ values for Er³⁺:Si₃N₄, Er³⁺:SiN_x, and Er³⁺:SiO₂

are 3×10^{-16} cm², 1×10^{-15} cm², and 3×10^{-14} cm², respectively (cf., Fig. 4). Similar values were already reported for Er³⁺:SiN_x,⁶ and the σ for Er³⁺:SiO₂ is among the highest excitation cross-sections reported in the literature.^{8,31} Comparable range of σ values can be obtained by investigating the dynamics of EL intensity of our samples (see supplementary material²¹).

To have an independent confirmation of the differences in excitation efficiency, we provide an evaluation of the number of excited Er³⁺ ions in each sample. One can roughly estimate a lower bound for the fraction of electrically excited Er³⁺ ions by using the following relation⁷: $\frac{N_{\text{Er}}^*}{[Er]} = A \frac{W_{\text{opt}} \tau}{h\nu S d}$, where A is a correction factor that takes into account both the total transmittance at 1.5 μm through the top polysilicon layer and the collection of the detection system (these combined effects reduce the detected power to 2% of the total emitted power for all investigated layers), W_{opt} is the detected optical power, τ the measured lifetime, $h\nu$ the energy of light emission, S the emitting area, and d the thickness of the active layer. While the fraction of excited Er³⁺ ions for SiN_x and Si₃N₄ are found to be 0.08% and 0.09%, respectively, it is significantly higher in SiO₂ for which it is estimated to be around 15%. Although potential clustering of erbium could limit the light emission in some cases,³² such a phenomenon would affect all samples equally as the same fabrication process and thermal treatment were used for all devices. Furthermore, we can infer on the basis of lifetime evolution versus current flux that nonlinear effects such as energy transfer could occur at high flux in Si₃N₄ but neither in SiN_x nor in SiO₂ (see supplementary material²¹). This phenomenon is therefore not responsible for the large differences in efficiencies between nitride and oxide hosts.

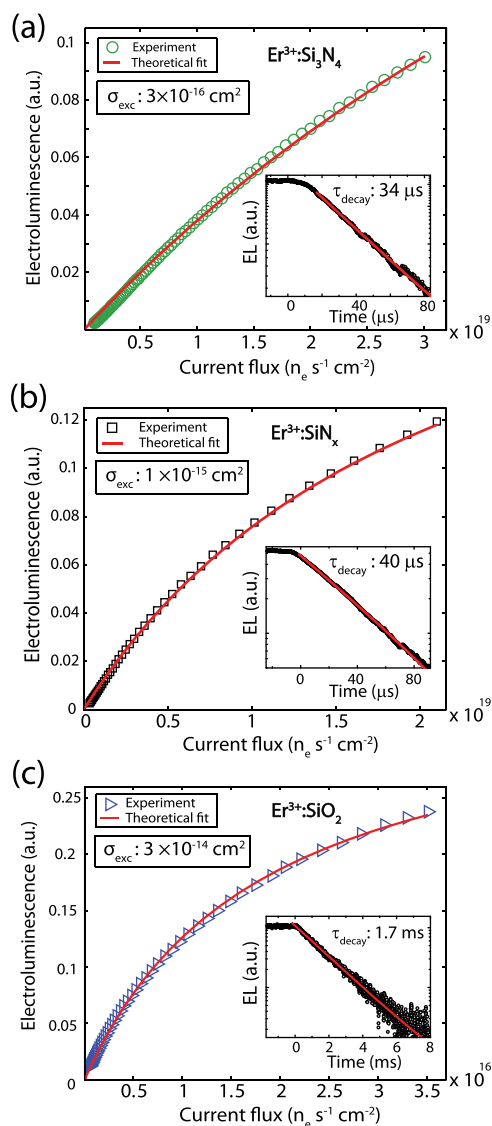


FIG. 4. Electroluminescence signal as a function of current flux for (a) $\text{Er}^{3+}:\text{Si}_3\text{N}_4$, (b) $\text{Er}^{3+}:\text{SiN}_x$, and (c) $\text{Er}^{3+}:\text{SiO}_2$ along with their corresponding theoretical fits to extract values of excitation cross-sections. Insets: measured lifetimes and fits.

Note that the low number of excited Er^{3+} ions in nitrogen-containing electroluminescent devices (Si_3N_4 and SiN_x) is correlated with the bulk-limited conduction mechanism in these materials. While this process allows for good conduction properties and low onset voltage for EL, it strongly reduces the excitation efficiency of Er^{3+} ions. In such a regime, the Er^{3+} excitation could occur via either energy transfer between traps and Er^{3+} ions^{6,8,10–12} or impact excitation.⁸ In the case of energy-transfer excitation, the donor-acceptor interaction is distance-dependent,³³ and the probability for such a process to occur is therefore low (Note that the fraction of excited Er^{3+} ions found here is comparable to the one for Er^{3+} ions sensitized by energy-transfer from Si nanoclusters.^{33,34}) On the other hand, potential impact excitation of Er^{3+} would require the injection of hot electrons having energies higher than the first excited state of Er^{3+} (0.8 eV). As measured by DiMaria *et al.*, the number of injected hot electrons in nitride-based layers is almost four-orders of magnitude lower than in a similar SiO_2 layer

because of electrical trapping.³⁵ Indeed, although FNT transport of carriers in SiO_2 yields a relatively low conductivity, it ensures the injection of a high number of hot carriers.^{35,36} Besides, as shown by Fischetti *et al.*,³⁶ in the range of electric fields applied in the present study (8–10 MV/cm), the energy of hot electrons in SiO_2 is distributed over an average value of around 3 eV, i.e., more than enough to pump the Er^{3+} ions to the first excited state by impact excitation. The significantly higher number of injected hot electrons in SiO_2 compared to nitride-based layers provides a straightforward explanation of the large differences in excitation cross sections and in the number of excited Er^{3+} ions. Interestingly, these correlations between electrical transport and excitation efficiencies can be inferred from the $\text{Er}^{3+}:\text{SiO}_2$ sample alone because it demonstrates both types of conduction mechanisms. Indeed the abrupt increase in Er^{3+} EL as soon as the FNT regime starts (Fig. 3(d)) provides a direct and striking confirmation of the higher efficiency of the hot carrier injection as compared to defect-assisted conduction for the excitation of Er^{3+} ions.

In conclusion, we have demonstrated that although both electrical conduction and onset voltage for the electroluminescence of Er^{3+} are greatly enhanced in nitrogen-containing Si-based samples, their excitation efficiencies are well below that of $\text{Er}^{3+}:\text{SiO}_2$. These results suggest that defect-assisted transport of carriers is a much less efficient process than hot electron injection for the electrical excitation of Er^{3+} . Despite the large excitation cross sections and EQE values for EL in $\text{Er}^{3+}:\text{SiO}_2$ electroluminescent devices, their very high onset voltage remains largely incompatible with current CMOS technology. On the other hand, the extremely low onset voltage for EL in $\text{Er}^{3+}:\text{SiN}_x$ appears very promising. Therefore, future studies should focus on electrical and material engineering to combine the advantages of both hosts to efficiently inject hot carriers at low voltages. In this framework, heterostructures composed of nanometer-thick multilayers appear to be a promising direction for investigation.³⁷

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